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ABSTRACT

This study explored the extent to which current adequate yearly progress (AYP) indices reflect real change or a statistical artifact. The objective, in more specific terms, was to investigate regression artifacts in evaluating schools' academic progress and explore methods to overcome their effects in developing AYP measures. Schools in Kentucky and Maine were studied, using eighth-grade achievement data from the two states' student assessments, the Kentucky Instructional Results Information System and the Maine Educational Assessment. Three different types of school achievement gain estimates were computed: (1) the 1-year gain measure; (2) a 2-year gain measure; and (3) a 3-year gain measure. Time-reversed analyses were conducted to determine whether gain score really was a regression artifact. Findings for both states show that higher performing schools tend to gain less while lower performing schools gain more. This illustrates the well-known regression to the mean status phenomenon. Results also reveal regression to the mean growth phenomenon. Schools that gained more in the past tend to gain relatively less. The first force tends to make higher and lower performing schools appear convergent in their status, and the latter force may make more and less improving schools appear convergent in their growth. These two forces as statistical artifacts may confound AYP measures and need to be addressed. (Contains 4 figures, 11 tables, and 9 references.) (SLD)

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ED 464 955

# How adequate are Adequate Yearly Progress (AYP) Measures?

## Regression artifacts and school AYP

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1. Research Questions and Objectives

The reauthorized Elementary and Secondary School Act (ESEA), No Child Left Behind Act, requires standards-based accountability for school systems receiving federal funds. One major component of this accountability policy is to require states and school districts to gradually demonstrate progress toward ensuring that all students are academically proficient—as defined by each state—within 12 years. This policy requires developing measures to evaluate individual schools' adequate yearly progress (AYP). Currently, there are substantial variations among the 50 states in terms of their operational definitions of AYP and, further, the data and methods employed to develop AYP measures (CPRE, 2000).

The dominant design for studying progress of schools across the nation is by means of successive-group comparisons (Carlson, 2001). This approach looks at the average achievement gain/loss from one year to the next for successive groups at the same grade level (e.g., comparing the average reading score of $4^{th}$ graders in 2002 with the average reading score of $4^{th}$ graders in 2001). Using this approach, one infers a change in the quality of a school or its programs by looking at the performance difference between two groups of students. Inherent weaknesses of this approach are initial group differences and mobility.

Hill (1997) has demonstrated that sampling error makes it difficult to determine which schools are making AYP and which are not. Pooling data from multiple grades and/or years may reduce these sampling errors, although more than three or four years of data may be required to draw a valid comparison. Researchers also have found that successive-group comparisons can produce results different from those based on longitudinal comparisons, where performance is followed over time for the same cohort of students (e.g., Carlson, 2001; Dyer et al., 1969). And

as Linn and Baker (1999) point out, within-school changes in student body can covary with changes in instruction, complicating the interpretation of AYP data.

Regression artifacts further complicate the evaluation of school AYP. Regression to the mean occurs when we examine the difference between two imperfectly correlated measures. Lower performing schools tend to improve their performance status more than higher performing schools. In other words, a school's baseline score (i.e., where the school started) is negatively correlated with the school's gain score (i.e., how much the school improved). We call this phenomenon *regression to the mean status*. Further, when we attempt to look at growth at more than two time points and examine growth in two adjacent periods, we may face another type of regression artifact: *regression to the mean growth*. For instance, if we choose to examine change from year 1 to year 2 and from year 2 to year 3, then the change from year 1 to year 2 will be negatively correlated with the change from year 2 to year 3. It is particularly problematic when one attempts to examine change in the growth between two periods: the "winners" in one period may appear to be "losers" in the other (and vice versa).

The central research question that we explore below is the extent to which current AYP indices reflect real change or a statistical artifact. Specifically, the objective of our study is to (a) investigate regression artifacts in evaluating schools' academic progress and (b) explore methods to overcome their effects in developing AYP measures. To date, little attention has been paid to regression artifacts and their possible implications for AYP evaluation.

## 2. Research Methods and Data

### Data

We examined schools in Kentucky and Maine. Early on, both states (a) established student assessment systems to monitor their schools' academic progress and (b) made a greater effort to align their assessments with the announced content and performance standards (Lee, 2000). We used 8th mathematics achievement data collected from the two states' student assessments: the Kentucky Instructional Results Information System (KIRIS) for 1993-1998 and the Maine Educational Assessment (MEA) for 1990-1998.

Figure 1 shows the distributions of MEA 8th grade math school scale scores from 1990 through 1998. MEA scores range from 100 to 400, with a mean of 250 and standard deviation of 50 in the 1985-1986 base year. Figure 2 shows the distributions of KIRIS 8th grade math school accountability index scores from 1993 through 1998. The KIRIS accountability index score is a weighted composite reflecting the percentage of students at four different achievement levels (0 for Novice, .4 for Apprentice, 1.0 for Proficient, and 1.4 for Distinguished). Thus, KIRIS accountability index scores can range from 0 to 140. Although the MEA and KIRIS use different types of school scores for reporting purposes, their underlying test scores are both equated across years so that we can see whether individual schools in each state have made academic progress over time.[1] While schools in both states appear to have made significant achievement gains over the period, there is substantial between-school variation in the amount of progress made.

Methods

We computed three different types of school achievement gain estimates: (a) the one-year gain measure computes the difference between two adjacent-year means (e.g., 1991-1992 gain = a school's 1992 mean minus its 1991 mean); (b) the two-year gain measure computes the

[1] Like Kentucky, Maine also employed criterion-referenced school performance reporting since 1995 and, since 1997, has calculated school AYP based on the weighted composite of the percentage of students at four different achievement levels. However, we do not use these data in this paper because they are available for only an

difference between adjacent two-year moving average scores (e.g., 9091-9293 gain = difference between the average of 1992 and 1993 means and the average of 1990 and 1991 means); and (c) the three-year gain measure computes the difference between adjacent three-year moving average scores (e.g., 9092-9395 gain = difference between the average of 1993, 1994, and 1995 means and the average of 1990, 1991, and 1992 means). We also conducted ordinary least-squares (OLS) time-series regression analyses of the school performance data over the entire periods, determining how the long-term trends compare with short-term gains.

Further, we conducted time-reversed analyses to determine whether gain score really is a regression artifact (see Campbell & Stanley, 1963; Campbell & Kenny, 1999). In order to remove regression artifacts from gain score, we conducted regressions of 1-year, 2-year, and 3-year gain scores on their corresponding baseline scores and preceding gain scores, and obtained residualized gains. As Cronbach and Furby (1970) pointed out earlier, the residualized gain score is a way of removing the effect of pretest status from posttest score but it is not a corrected measure of true change because the portion discarded may include some genuine and important changes in the subjects (in this case, schools). Despite the limitations of residualized gain scores (Cronbach & Furby, 1970), we incorporated them in our analyses to explore how they might address regression artifacts and how this adjustment might improve the relationships among raw gain scores.

## 3. Research Findings and Implications

Analysis of school means and their relationship

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insufficient number of years. Also we do not examine any post-1998 data here because both states have used a new student assessment since 1999, rendering the earlier data incomparable.

Correlations among one-year school means of 8th grade math achievement are modestly positive (see Table 1). The correlation coefficients are in the .40s and .50s for adjacent years, and they become weaker for remote years. For example, the correlation between 1990 and 1991 means is .55, while the correlation between 1990 and 1998 means is .34. This indicates proximal autocorrelation in the time-series data (Campbell & Kenny, 1999). These generally modest correlations indicate that one-year school mean scores are not stable, and even diminishing correlations indicate that the estimate of school performance based on one-year means may lose its stability further over time.

Correlations among two-year school means of 8th grade math achievement are in the .60s and .70s (see Table 2). The correlations among 2-year means are generally higher than the correlations among one-year means, indicating that the former increases stability by combining two years' data. Likewise, correlations among three-year school means of 8th grade math achievement are also slightly higher than correlations among two-year school means (see Table 3). As one would expect, the correlations among two-year or three-year means are particularly high when the two adjacent periods have common years. However, proximal autocorrelation still prevails: the size of correlation coefficients drop substantially as the time periods grow further apart.

Analysis of school gains and their relationship

Now we obtain three different types of gain scores for each school by computing differences among one-year means, among two-year means, and among three-year means. In this section, we examine the relationship among successive gain scores to find out whether the schools' gain scores are stable over time. If current AYP measures are to serve as a reliable indicator of school effectiveness, then school gains should demonstrate stability as evidenced by

positive correlations among successive gains. We understand that being reliable doesn't guarantee the validity of the AYP measures used, but it should be one of necessary conditions for demonstrating their validity.

Table 4 shows correlations among one-year gains. Correlations among yearly gain scores are very low for close pairs remote pairs alike. In other words, schools that appear to gain more this year do not maintain their gains the following years. The only exception is the moderately negative correlation between adjacent periods with an overlapping year (see the correlations in central diagonal line in Table 4). For example, the correlation between 9091 gain and 9192 gain is -.45. This is likely to result from the fact that both gains share the 1991 score with different signs, that is, plus 91 score in 9091 gain versus minus 91 score in 9192 gain. Aside from the artifactual, inverse relationship between adjacent pair of gains, the overall patterns of correlations indicate that there is no stability in the amount of yearly gain scores made by schools.

The correlations among two-year gains are somewhat higher than the correlations among one-year gains (see Table 5). However, the higher correlations are observed only when the two periods involve common years. Moreover, the correlations are often negative for the same reason as one-year gain correlations above. When we look at two periods with no common years (e.g., 9091-9293 gain vs. 9596-9798 gain), the correlations are barely significant. The correlations among three-year gains may be more stable (see Table 6), but they tend to have the same problems as the correlations among two-year gains.

To examine a longer-term trend in schools' academic progress, we ran OLS time-series linear regression to obtain the estimate of annual school gain over the entire period in each state: 9 years in Maine and 6 years in Kentucky. Among the 224 Maine schools with enough data for

this regression, 85 schools (38%) had statistically significant gain estimates. The average of all 224 schools' annual gain estimates is 7.72, or .12 standard deviations (based on the 1990 standard deviation). Among the 315 Kentucky schools with enough data for this regression, 140 schools (44%) had statistically significant gain estimates. The average of all 315 schools' annual gain estimates is 5.34, or .47 standard deviations (based on the 1993 standard deviation).

In order to find out how well these different types of gains reflect the long-term trend, we examined the correlations between the former and the latter. Table 7 shows that three-year gain provides a closer estimate of the long-term academic growth trend than does two-year gain, which in turn is better than one-year gain. The correlations between three-year gains and whole-period trends are in the .50s and .60s. This indicates that AYP measures require longer intervals of data to provide a better approximation of the long-term trend. Nevertheless, it is uncertain whether an estimate of even a longer-term trend can provide a satisfactorily reliable and valid assessment of schools' academic progress.

Regression artifacts and residualized gains

Correlations between initial status and gain scores are modestly negative (ranging mostly from -.40s to -.50s), which suggests that lower performing schools tend to gain more than higher performing schools. This might suggest the well-known regression to the mean artifact. We call this type of regression artifact *regression to the mean status*, which we distinguish from another type of regression artifact explained below. We conducted time-reversed analyses of gain score to determine whether it really is a regression artifact. Schools were classified into three groups (top quartile, middle half, bottom quartile) based on their 8$^{th}$ grade math mean scores in each of two adjacent years, and their performance trajectories were compared.

Figure 3 illustrates regression to the mean status with 1996 and 1997 data from Maine. Forward performance trajectories (solid lines) trace changes in average scores from 1996 to 1997 for three groups of schools that were classified based on their 1996 performance status: high (96 H), middle (96 M), and low (96 L). In contrast, backward performance trajectories (broken lines) trace changes from 1997 to 1996 for three groups of schools that were classified based on their 1997 performance status: high (97 H), middle (97 M), and low (97 L). For both high and low performing schools, backward trajectories turn out to move in the same direction as their forward counterparts.[2] For instance, high performing schools in 1996 perform less well (going downward) in 1997, but at the same time high performing schools in 1997 also turn out to perform less well in 1996. This time-reversed analysis strongly indicates a regression artifact.

Correlations among yearly gain scores for adjacent years are also negative (ranging from -.30s to -.50s). Schools that gained more in the current year tend to gain less in the next year. This suggests another type of regression artifact. The same is true of two-year and three-year gains, which also show a negative relationship with adjacent year gains (i.e., either two-year or three-year). This type of regression artifact, which we call *regression to the mean growth*, is illustrated in Figure 4. Here, schools were classified into three groups based on their achievement gains in 1995-96 and in 1996-97. Once again, forward vs. backward trajectories for high (H) and low (L) improving schools also turn out to move in the same directions. If there had been no regression artifact, forward and backward trajectories would have followed the opposite directions.

We found that the regression-to-the-mean-growth effect operates independent of

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[2] If backward trajectories are traced from 1996 to 1997, then they appear to move in the opposite directions to forward trajectories. But backward trajectories by definition should be viewed as moving from 1997 to 1996.

regression-to-the-mean-status effect. Further, the former is often as strong as the latter. For example, Table 8 shows the results from two separate, multiple regression analyses of the 1995-1997 data from Maine schools, one using regular (forward) regression and another using time-reversed (backward) regression. For time-reversed regression, we used both current period's gain and baseline score to predict previous period's gain. In this case, both forward and backward regression analyses produce very similar results: The effects of both predictors are significantly negative. If there had been no regression artifacts, the effects should have weakened substantially or disappeared altogether. We conducted the same analysis for 2-year and 3-year gains, obtaining similar results.

Given these prevailing regression artifacts, we attempted to obtain estimates of school gains that are not influenced by these misleading effects. We ran a series of forward regressions as shown in the top part of Table 8 to obtain residuals. Table 9 shows correlations among residualized one-year gains. Values in parentheses show changes in correlation coefficients compared with those in Table 4. Although all of the correlations change in a more positive direction, the changes are quite marginal; negative correlations become less negative, but hardly change into positive. Likewise, Table 10 and Table 11 respectively show correlations among 2-year and 3-year residualized gains. The same tendency of changes in correlation coefficients are found.

Many researchers claimed that regression to the mean is more of a problem for two-wave studies than multiwave studies. But Campbell and Kenny (1999) point out that the empirical fact of proximal autocorrelation implies that regression to the mean continues after the second wave of measurement. It is true that the largest amount of regression toward the mean usually takes place at lag 1 because that is where the correlation changes most. However, regression to the

mean continues because the correlation keeps dropping further after lag 1. Thus, however many time points we look at for an estimation of change or trend, it is necessary to take cautionary steps against regression artifacts.

Policy and Research Implications

Both Kentucky and Maine adopted the method of successive-group comparisons (i.e., comparing the performance of different cohorts) to evaluate school AYP. Previous studies and the present findings strongly challenge the validity of current AYP measures based on this method. Although the most important source of instability in school performance gain may come from changes in student body and mobility, neither factor is considered in developing and evaluating school AYP measures. Indeed, the lower reliability of gain scores due to large sampling error and resulting lower correlations among the gain scores should worsen regression artifacts. But we suspect that these regression artifacts may remain legitimate concerns due to measurement error even if states could switch to a longitudinal-comparison design (i.e., following the performance of the same students).

In summary, our findings show that higher performing schools tend to gain less while lower performing schools gain more. This illustrates the well-known regression to the mean "status" phenomenon. At the same time, our results also reveal regression to the mean "growth" phenomenon. Schools that gained more than others in the past tend to gain relatively less. The former force tends to make higher and lower performing schools appear convergent in their status, whereas the latter force may make more and less improving schools appear convergent in their growth. These two forces as statistical artifacts may confound school AYP measures and need to be addressed. At the same time, it is important to realize that any adjustment for

regression artifacts cannot cure the underlying problems with current AYP measures that arise from the use of successive comparison method.

Kentucky was among the first states to establish a clear definition of adequate yearly progress as part of a state accountability system (Linn & Baker, 1999). Their timeline for AYP has changed along with a new assessment system. According to the state's new AYP rule, every school has to meet the goal of 100 by 2014; this goal can be accomplished when schools have 100% of their students perform at proficient level. Schools get a composite accountability index score based on percent students at each of the four achievement levels (novice, apprentice, proficient, and distinguished) and they are expected to fill the gap between their current score and the goal of 100 (one seventh of the gap each biennium). Schools may receive rewards or assistance depending on whether they met the AYP quota.

In contrast, Maine developed AYP measures to evaluate only Title I schools and adopted a transitional formula to evaluate a school's AYP status. According to the current rule, schools that have over 70% of students who do not meet the state standards and an average scale score of 535 or lower for two consecutive years are designated as "priority" or "needs improvement" schools. Those schools are eligible to receive technical assistance from the state and need to demonstrate progress by making a 3-5 point gain on the MEA scale for two consecutive years.

Do these two AYP approaches make sense, given the regression artifacts that we have considered in this paper? In the case of Maine, they set the same quota for all Title I schools, despite the fact that there are substantial variation among even those relatively low-performing schools. In case of Kentucky, they set different quota for schools according to the schools' baseline status. Schools that initially performed at a lower level would be assigned a task of making relatively large gains—that is, meeting a higher AYP threshold—while initially higher

performing schools would have to meet a relatively lower AYP threshold. The Kentucky approach has the potential to take into account the regression-to-the-mean-status artifact, but it is not clear whether this adjustment is reasonable and how it differs from the residualized gain approach. To test this, subsequent research may compare individual schools' adjusted gain scores (residuals obtained after controlling for the effect of initial score) with their AYP difference score (difference between school-specific AYP threshold and actual gain made) and with their raw gain.

On the other hand, the effect of regression to the mean growth is not considered by the current AYP formula for either Kentucky or Maine. Once the AYP threshold or quota for each school is set based on the gap between baseline performance and expected performance, it does not change. So schools have to meet the same quota every period regardless of how much progress they made previously. In both states, the AYP quota for schools does not change as their scores change. An arguably more sensible approach is to reset the AYP quota every time, adjusting for the amount of progress toward the goal. This way, schools that improved more than the quota and thus narrowed the gap more would be assigned a smaller quota next time. This has the potential to address the regression-to-the-mean-growth artifact. To test how this works, subsequent research may compare individual schools' adjusted gain scores (residuals obtained after controlling for the effect of previous gain) with their adjusted AYP difference score (gap between moving AYP threshold and actual gain) and with their unadjusted AYP difference score (gap between fixed AYP threshold and actual gain).

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Table 1. Correlations among one-year school means of 8th grade mathematics achievement in Maine and Kentucky

| | 1991 mean | 1992 mean | 1993 mean | 1994 mean | 1995 mean | 1996 mean | 1997 mean | 1998 mean |
|---|---|---|---|---|---|---|---|---|
| 1990 mean | .55 | .47 | .41 | .44 | .51 | .46 | .28 | .34 |
| 1991 mean | | .50 | .52 | .54 | .45 | .43 | .41 | .30 |
| 1992 mean | | | .59 | .65 | .51 | .48 | .39 | .49 |
| 1993 | | | | .65 | .53 | .41 | .42 | .47 |
| mean | | | | .62 | .56 | .64 | .67 | .62 |
| 1994 | | | | | .60 | .54 | .50 | .50 |
| mean | | | | | .59 | .60 | .56 | .57 |
| 1995 | | | | | | .65 | .52 | .45 |
| mean | | | | | | .62 | .61 | .58 |
| 1996 | | | | | | | .48 | .49 |
| mean | | | | | | | .72 | .65 |
| 1997 | | | | | | | | .56 |
| mean | | | | | | | | .76 |

Note. Upper values are for Maine schools in 1990-1998 and lower values are for Kentucky schools in 1993-1998.

Table 2. Correlations among two-year school means of 8th grade mathematics achievement in Maine and Kentucky

| | 9192 mean | 9293 mean | 9394 mean | 9495 mean | 9596 mean | 9697 mean | 9798 mean |
|---|---|---|---|---|---|---|---|
| 9091 mean | .83 | .60 | .61 | .63 | .59 | .51 | .46 |
| 9192 mean | | .85 | .74 | .69 | .59 | .54 | .54 |
| 9293 mean | | | .89 | .73 | .58 | .51 | .57 |
| 9394 mean | | | | .87<br>.84 | .62<br>.74 | .58<br>.74 | .61<br>.71 |
| 9495 mean | | | | | .85<br>.90 | .58<br>.72 | .61<br>.69 |
| 9596 mean | | | | | | .85<br>.88 | .64<br>.76 |
| 9697 mean | | | | | | | .84<br>.90 |

Note. Upper values are for Maine schools in 1990-1998 and lower values are for Kentucky schools in 1993-1998.

Table 3. Correlations among three-year school means of 8th grade mathematics achievement in Maine and Kentucky

| | 9193 mean | 9294 mean | 9395 mean | 9496 mean | 9597 mean | 9698 mean |
|---|---|---|---|---|---|---|
| 9092 | .91 | .81 | .74 | .72. | .60 | .59 |
| mean | | | | | | |
| 9193 | | .93 | .85 | .72 | .60 | .60 |
| mean | | | | | | |
| 9294 | | | .93 | .81 | .64 | .64 |
| mean | | | | | | |
| 9395 | | | | .91 | .77 | .69 |
| mean | | | | .95 | .89 | .79 |
| 9496 | | | | | .91 | .82 |
| mean | | | | | .85 | .86 |
| 9597 | | | | | | .91 |
| mean | | | | | | .94 |

Note. Upper values are for Maine schools in 1990-1998 and lower values are for Kentucky schools in 1993-1998.

Table 4. Correlations among one-year gains of 8th mathematics achievement in Maine and Kentucky

| | 9192 gain | 9293 gain | 9394 gain | 9495 gain | 9596 gain | 9697 gain | 9798 gain |
|---|---|---|---|---|---|---|---|
| 9091 gain | -.45 | .08 | -.05 | -.16 | .02 | .13 | -.12 |
| 9192 gain | | -.49 | .01 | -.07 | -.05 | -.02 | .16 |
| 9293 gain | | | -.51 | .04 | -.10 | .07 | -.02 |
| 9394 gain | | | | -.39<br>-.34 | .10<br>-.07 | -.10<br>-.12 | -.09<br>.08 |
| 9495 gain | | | | | -.34<br>-.57 | -.09<br>.04 | -.06<br>-.06 |
| 9596 gain | | | | | | -.44<br>-.39 | .12<br>-.07 |
| 9697 gain | | | | | | | -.51<br>-.37 |

Note. Upper values in each cell are for Maine schools in 1990-1998 and lower values are for Kentucky schools in 1993-1998.

Table 5. Correlations among two-year gains of 8th mathematics achievement in Maine and Kentucky

| | 9192-9394 gain | 9293-9495 gain | 9394-9596 gain | 9495-9697 gain | 9596-9798 gain |
|---|---|---|---|---|---|
| 9091-9293 gain | .39 | -.48 | -.40 | -.19 | .08 |
| 9192-9394 gain | | .26 | -.35 | -.31 | -.02 |
| 9293-9495 gain | | | .49 | -.12 | -.28 |
| 9394-9596 gain | | | | .48<br>.22 | -.40<br>-.45 |
| 9495-9697 gain | | | | | .32<br>.42 |

Note. Upper values in each cell are for Maine schools in 1990-1998 and lower values are for Kentucky schools in 1993-1998.

Table 6. Correlations among three-year gains of 8th mathematics achievement in Maine and Kentucky

| | 9193-9496 gain | 9294-9597 gain | 9395-9698 gain |
|---|---|---|---|
| 9092-9395 gain | .51 | .06 | -.30 |
| 9193-9496 gain | | .68 | .30 |
| 9294-9597 gain | | | .69 |

Note. All values are for Maine schools in 1990-1998; values for Kentucky schools are not shown as their data are available only in 1993-1998.

Table 7. Correlations of long-term trend regression coefficient with 1-year, 2-year, and 3-year gain scores

| 1-year gain | | 2-year gain | | 3-year gain | |
|---|---|---|---|---|---|
| 9091 | .12 | 9091-9293 | .44 | 9092-9395 | .62 |
| gain | | gain | | gain | |
| 9192 | .29 | 9192-9394 | .45 | 9193-9496 | .66 |
| gain | | gain | | gain | |
| 9293 | .10 | 9293-9495 | .42 | 9294-9597 | .51 |
| gain | | gain | | gain | |
| 9394 | .17 | 9394-9596 | .34 | 9395-9698 | .47 |
| gain | .34 | gain | .44 | gain | .58 |
| 9495 | .22 | 9495-9697 | .30 | | |
| gain | .19 | gain | .62 | | |
| 9596 | .17 | 9596-9798 | .32 | | |
| gain | .22 | gain | .56 | | |
| 9697 | .16 | | | | |
| gain | .30 | | | | |
| 9798 | -.03 | | | | |
| gain | .18 | | | | |

Note. Upper values in each cell are for Maine schools in 1990-1998 and lower values are for Kentucky schools in 1993-1998.

Table 8. Forward vs. backward regression of 1-year school gain score in Maine

| Regression of 9697 gain on 9596 gain and 96 mean | | | | | |
|---|---|---|---|---|---|
| | Coefficient | Standard Error | Beta | t | p-value |
| Intercept | 150.84 | 19.200 | | 7.856 | .000 |
| 96 mean | -.416 | .057 | -.437 | -7.317 | .000 |
| 9596 gain | -.281 | .061 | -.273 | -4.580 | .000 |
| Adjusted $R^2$ = .348 | | | | | |
| **Regression of 9695 gain on 9796 gain and 96 mean** | | | | | |
| | Coefficient | Standard Error | Beta | t | p-value |
| Intercept | 37.768 | 23.258 | | 1.624 | .106 |
| 96 mean | -.177 | .067 | -.192 | -2.641 | .009 |
| 9796 gain | -.323 | .071 | -.332 | -4.580 | .000 |
| Adjusted $R^2$ = .208 | | | | | |

Note. 9697 gain = 97 mean – 96 mean; 9796 gain = 96 mean – 97 mean; 9596 gain = 96 mean – 95 mean; 9695 gain = 95 mean – 96 mean.

Table 9. Correlations among one-year residualized gains of 8th mathematics achievement in Maine and Kentucky

| | 9192 gain | 9293 gain | 9394 gain | 9495 gain | 9596 gain | 9697 gain | 9798 gain |
|---|---|---|---|---|---|---|---|
| 9091 gain | -.11(+.34) | .23 (+.15) | .13 (+.18) | -.01(+.15) | .11 (+.09) | .22 (+.09) | .01 (+.13) |
| 9192 gain | | -.13(+.36) | .22 (+.21) | .10 (+.17) | .11 (+.16) | .16 (+.18) | .31 (+.15) |
| 9293 gain | | | -.26(+.25) | .09 (+.05) | -.03(+.07) | .16 (+.09) | .12 (+.14) |
| 9394 gain | | | | -.17(+.22)<br>-.34 (-.20) | .20 (+.10)<br>.12 (+.19) | -.10 (.14)<br>-.12 (.00) | .09(+.18)<br>..13(+.05) |
| 9495 gain | | | | | -.16(+.18)<br>-.23(+.24) | .09 (+.18)<br>.15 (+.11) | .02 (+.08)<br>.07 (+.13) |
| 9596 gain | | | | | | -.15(+.29)<br>-.18(+.21) | .24 (+.12)<br>.06 (+.13) |
| 9697 gain | | | | | | | -.17(+.34)<br>-.19(+.18) |

Note. Upper values in each cell are for Maine schools in 1990-1998 and lower values are for Kentucky schools in 1993-1998. Values in parenthesis show changes in correlation coefficients (compared with Table 4) by adjusting for regression artifacts.

Table 10. Correlations among two-year residualized gains of 8th mathematics achievement in Maine and Kentucky

| | 9192-9394 gain | 9293-9495 gain | 9394-9596 gain | 9495-9697 gain | 9596-9798 gain |
|---|---|---|---|---|---|
| 9091-9293 gain | .49 (+.10) | -.17 (+.31) | -.11 (+.29) | -.04 (+.15) | .23 (+.15) |
| 9192-9394 gain | | .38 (+.14) | .-14 (+.21) | .-18 (+.13) | .13 (+.15) |
| 9293-9495 gain | | | .53 (+.04) | -.04 (+.08) | .10 (+.38) |
| 9394-9596 gain | | | | .49 (+.01)<br>.29 (+.07) | -.23 (+.17)<br>-.26 (+.19) |
| 9495-9697 gain | | | | | .42 (+.10)<br>.51 (+.09) |

Note. Upper values in each cell are for Maine schools in 1990-1998 and lower values are for Kentucky schools in 1993-1998. Values in parenthesis show changes in correlation coefficients (compared with Table 5) by adjusting for regression artifacts.

Table 11. Correlations among three-year residualized gains of 8th mathematics achievement in Maine and Kentucky

| | 9193-9496 gain | 9294-9597 gain | 9395-9698 gain |
|---|---|---|---|
| 9092-9395 gain | .57 (+.06) | .21 (+.15) | -.13 (+.17) |
| 9193-9496 gain | | .71 (+.03) | .34 (+.04) |
| 9294-9597 gain | | | .67 (+.02) |

Note. All values are for Maine schools in 1990-1998; values for Kentucky schools are not shown as their data are available only in 1993-1998. Values in parenthesis show changes in correlation coefficients (compared with Table 6) by adjusting for regression artifacts.

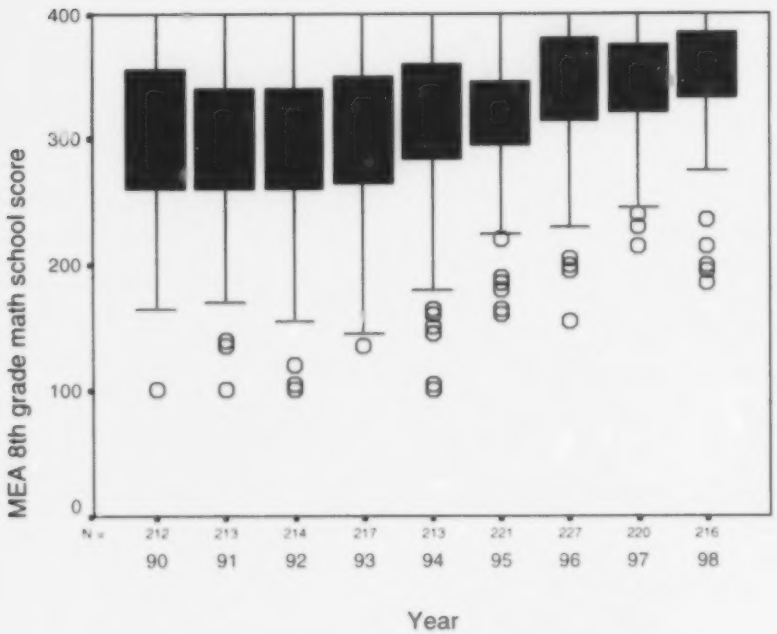


Figure 1. Box Plot of 1990-98 MEA 8th grade math school scores

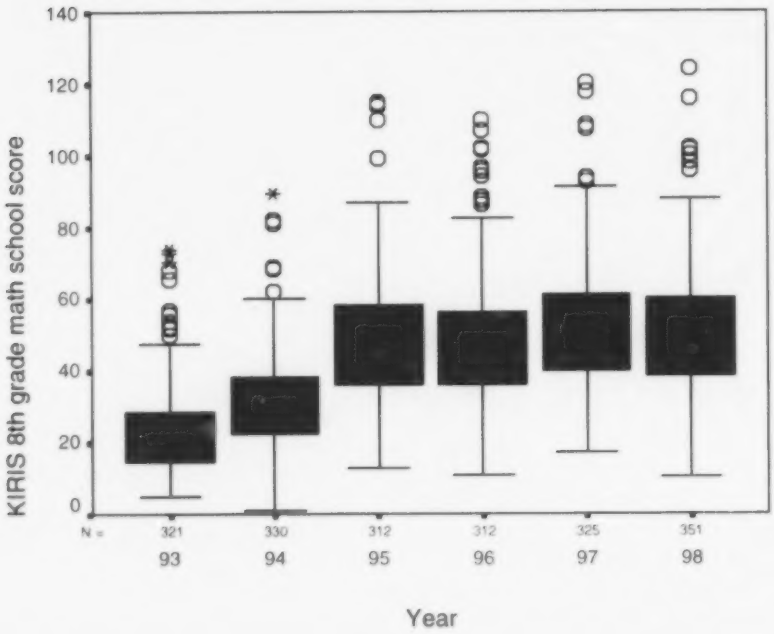


Figure 2. Box Plot of 1993-98 KIRIS 8th grade math school scores

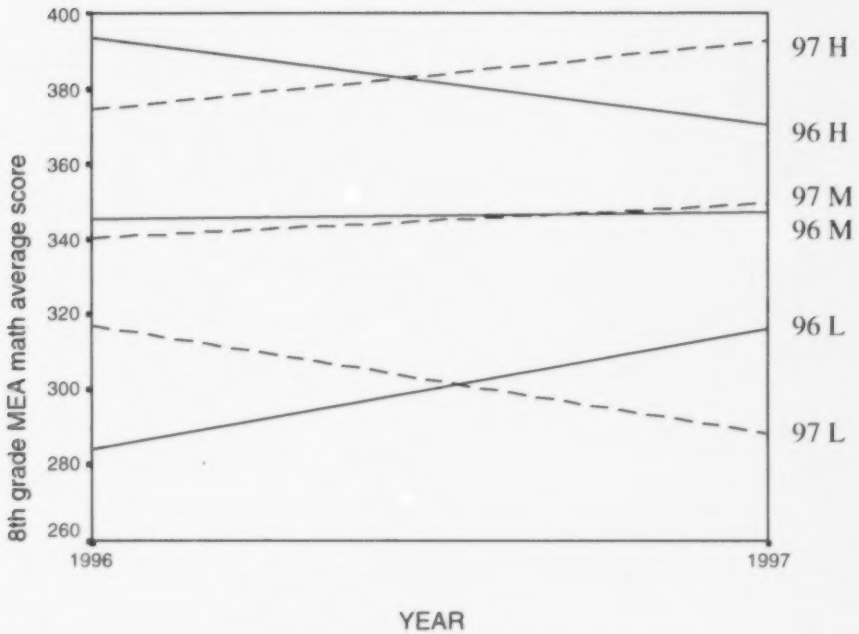


Figure 3. Forward vs. backward trajectories of 1996 and 1997 MEA 8th grade math school scores (YY H=high performing schools in year YY; YY M=middle performing schools in year YY; YY L=low performing schools in year YY)

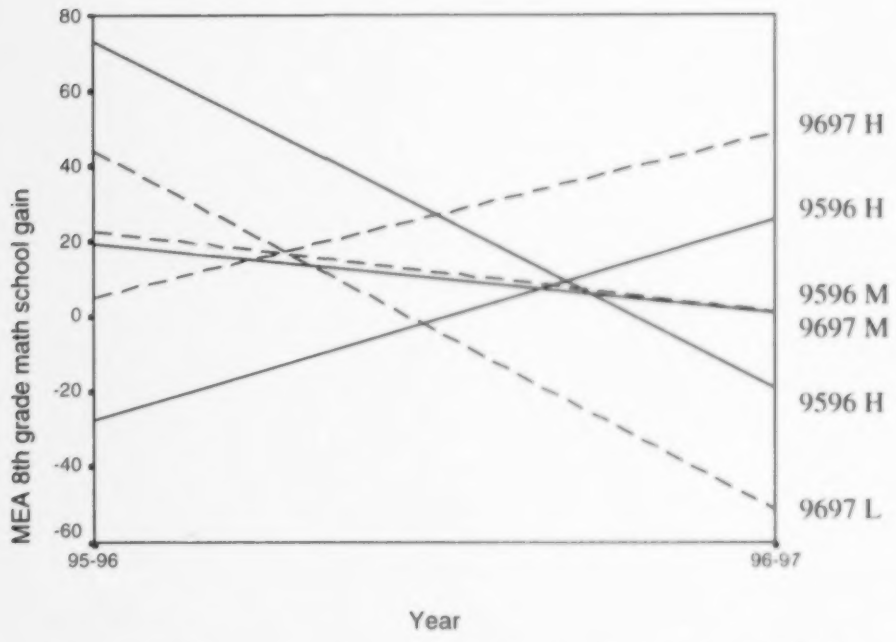


Figure 4. Forward vs. backward trajectories of 1995-96 and 1996-97 MEA 8th grade math school gains (XXYY H=high improving schools between years XX and YY; XXYY M=middle improving schools between year XX and YY; XXYY L=low improving schools between years XX and YY)